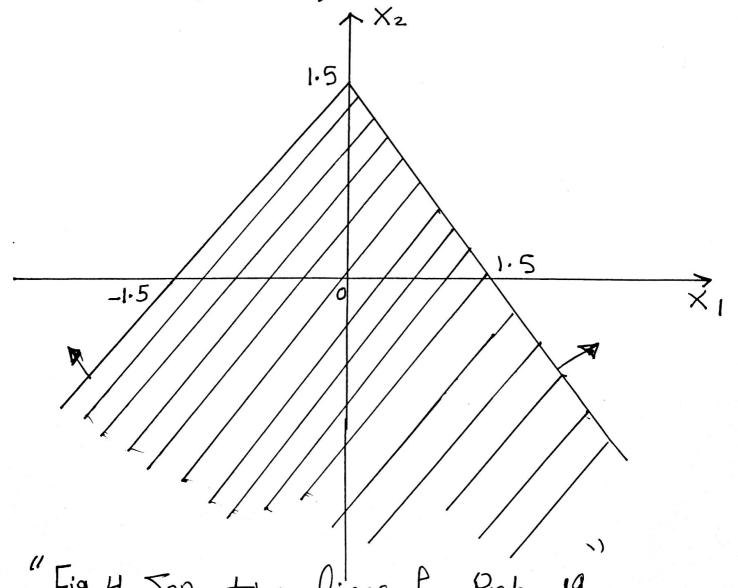
IS Consider the neural network of fig. 3, with an input data pattern (XI,X2) and an output signal. S. All neurons of the hidden and output layers Produce binary threshold signals. Find the various weights of the network such that it behaves as a two-class data classifier with the two separation lines shown in Fig. 4. The points within the hatched region are identified by S=0, and the points outside this region are identified by S=1. How will the input data patterns (0.5, 0.5), (0.5, 1.5) (0,2), and (0.9, 1.3) be classified?



"Fig. 4 Jeparation lines for Prob and

20] Consider the neural network of Fig. 3, with an input data Pattern (X1, X2) and an output signal 5. All neurons of the hidden and output layers produce binary threshold signals. Find the various weights of the Network such that it behaves as atwo-class data classifier with the separation lines shown in Fig. 5. The points within the hatched region are identified by 5=0, and the Points outside this region are identified by s=1. How will the following input data patterns be classified ? (-1, 1) (-1, -1) (1, 2.4)(-0.6,2.7) (0.8,0.5) (0,1.9)

Fig. 5 Jeparation lines for Prob. 20

## Problem 21

Consider the neural network of Fig. 3, with an input data pattern  $(x_1, x_2)$  and an output signal s. All neurons of the hidden and output layers produce binary threshold signals. The numerical values of the bias weights  $w_3$  and  $w_4$  are 1.0 and 0.8, respectively. Find the various weights of the network such that it behaves as a two-class data classifier with the separation lines shown in Fig. 6. The points within the hatched region are identified by s=1, and the points outside this region are identified by s=0. How will the input data patterns (2,0), (2,4), (-4,4), and (-4,-5) be classified?

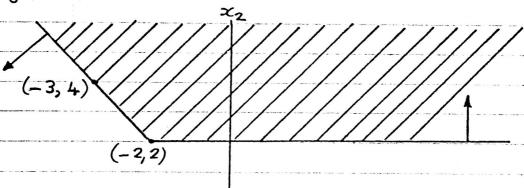


Fig. 6 Separation lines for Prob. 21

## Solution

The first separation line [passing through points (-2,2)
and (-3,4)] is

$$\frac{x_2-2}{x_1+2} = \frac{4-2}{-3+2}$$

22 Consider the neural network of Fig. 3, with an input data Pattern (x, x2) and an output signal S. All neurons of the hidden and output layers produce binary threshold signals. The numerical values of the bias weights was and way are o.7 and o.4, respectively. Find the various weights of the network such that it behaves as atwo-class data classifier with the separation lines shown in Fig. 7. The points within the hatched region are identified by s=1, and the Points atside this region are identified by S=0. How will the input data Patterns (0,0), (0,3), (2,2), and (2,-2) be classified?

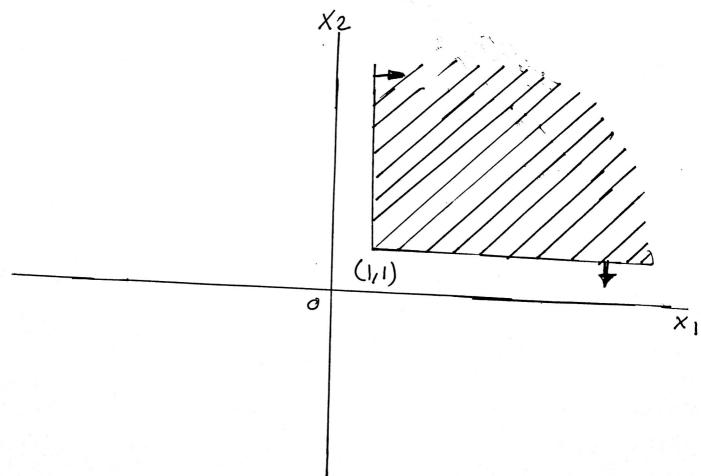


Fig. 7 Separation lines for Prob. 22.

## Problem 23

The neural network of Fig. 8 has an input data pattern  $(x_1, x_2)$  and an output signal s. All neurons of the hidden and output layers produce binary threshold signals. The weight values are:

$$w_{13} = -1$$
 ,  $w_{23} = 0.5$  ,  $w_{03} = 0.5$   
 $w_{14} = 0$  ,  $w_{24} = -0.8$  ,  $w_{04} = 0.8$   
 $w_{15} = 0.2$  ,  $w_{25} = 0.2$  ,  $w_{05} = -1$   
 $w_{36} = 1$  ,  $w_{46} = 1$  ,  $w_{56} = 1$   
 $w_{15} = 0.5$ 

(a) Show that the network can behave as a two-class data classifier on the  $x_1-x_2$  plane, where all points within a triangle with vertices (1,1), (2,3), and (4,1) are identified by s=0, and all points outside this triangle are identified by s=1.

(b) How will the input data patterns (2,2), (2,-2), (-1,1.5), and (5,3) be classified?

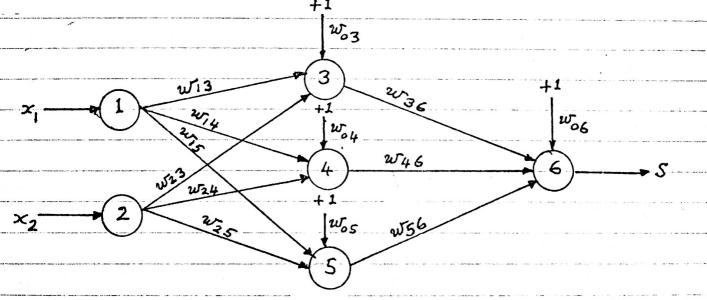


Fig. 8 Neural network for Prob. 23

24) Consider the neural network of Fig. 8, with an input data Pattern (X1, X2) and an output signal s. All neurons of the hidden and output layers Produce binary threshold Signals. The weight Values are:  $W_{13} = 0.3$ ,  $W_{23} = -0.7$ ,  $W_{03} = 0.2$  $W_{14} = 0$  ,  $W_{24} = 1$  ,  $W_{04} = 1$   $W_{15} = 0.25$  ,  $W_{25} = 0$  ,  $W_{05} = -1$ W36 = 0.8 , W46=0.7, W56 = -0.4 a) show that the network can behave as a two-class data classifier on the XI-Xz Plane, where all Points with in a specific right-angled triangle are Edentified by s=1, and all Points outside this triangle are identified by 5=0.

b) Determine the vertices of the triangle referred to in Part (a). c) what logic operation is performed by neuron 6 on the Jignals produced by Neurons 3, 4 and 5? d) How will the input data patterns (0,0) s (2,0), (4.5,0), and (-3.6,1.7) be

Classified ?

Problem 25

Consider the neural network of Fig. 8, with an input data pattern  $(x_1, x_2)$  and an output signal s. All neurons of the hidden and output layers produce binary threshold signals. Find the various weights of the network such that it behaves as a two-class data classifier. All points within the triangle shown in Fig. 9 are identified by s = 0, and all points outside this triangle are identified by s = 1. The numerical value of any bias weight should not exceed 1.5. How will the input data patterns (0,0), (2,0), (4,-1), and (-4,1) be classified?

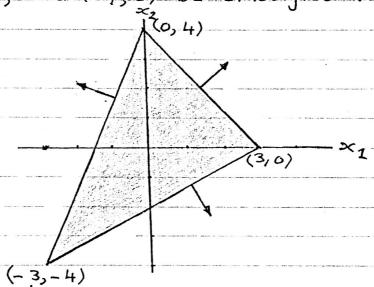


Fig. 9 Separation lines for Prob. 25

Solution

The first separation line [passing through points (0,4) and (-3,-4)] is

$$\frac{x_2-4}{x_1-0} = \frac{-4-4}{-3-0}$$

or

 $3x_2 = 8x_1 + 12$ 

Problem 27 (a) State a mathematical formula for calculating the number of linear dichotomies that can be induced on p points (in general position) in an n-dimensional space, L(p,n). (b) Use the formula of part (a) to show that L(4,3) = L(4,2) + 2(c) In view of the result of part (b), show that the logic XOR function can be implemented by the neural network of Fig. 10, where the space dimension increases from 2 to 3. Specify the role played by neuron 3, and determine the various weights of the network. (d) In part (c), portray the separation plane in the 3-dimensional space. Comment on this situation from the dichotomization viewpoint.

Fig. 10 Neural network for Prob. 27, part (c)

## Solution

(a) The mathematical formula for L(p,n) is

- 26) Repeat Prob. 25 when the orientations of the Separation lines are reversed.
- 28 In your solution of prob. 27, Part (c), specify the region of input patterns (x1, x2) for which:
- a)  $X_3 = 0$
- b) X3 = 1
- c)  $X_3 = 0$  and S = 0
- d) X3 = 0 and S = 1
- e)  $X_3 = 1$  and S = 0
- f)  $x_3 = 1$  and s = 1
- g) S=0
- h) 5=1
- 29 Repeat parts (c) and (d) of prob.27 and Prob.28 for the logic XNOR function.